# Overview of Modern ML Applications: Convolutional Neural Network (CNN)

Learning objectives

- o Describe the structure of CNN
- o Build and train simple CNNs using a deep learning package (Ref: Ch 9 of [Goodfellow et al. 2016\)](https://www.deeplearningbook.org/)

Acknowledgment: Some graphics and slides were adapted from Stanford's CS231n by Fei-Fei Li et al.: http://cs231n.stanford.edu/ F22v2

# Convolutional Neural Network (CNN)

The **single** most important technology that fueled the rapid development of **deep learning** and **big data** in the past decade.



LeCun, Bottou, Bengio, Haffner, "Gradient-Based Learning Applied to Document Recognition," *Proc. IEEE*, **1998**. 2

# Why is Deep Learning so Successful?

- 1. Improved model: convolutional layer, more layers ("deep"), simpler activation (i.e., ReLU), skip/residual connection (i.e., ResNet), attention (i.e., Transformer)
- **2. Big data:** huge dataset, transfer learning
- 3. Powerful computation: graphical processing units (GPUs)
- Example of big data: ImageNet (22K categories, 15M images)



Deng, Dong, Socher, Li, Li & Fei-Fei, "ImageNet: A Large-Scale Hierarchical Image Database," *IEEE CVPR*, 2009. 3

# **IMAGENET Large Scale Visual Recognition Challenge**

The Image Classification Challenge: 1,000 object classes 1,431,167 images



#### Linear Model to Neural Network

Re call linear model 
$$
\omega
$$
/ multiple predicts / features/inputs.  
\n
$$
\frac{y_{i}}{1} = \sum_{i=1}^{p} x_{ij} \beta_{i} + e_{i} = [\beta_{1}, ..., \beta_{P}] \begin{pmatrix} x_{i} \\ \vdots \\ x_{ip} \end{pmatrix} + e_{i}, i = 1, ..., n
$$
\n
$$
\frac{y_{i}}{1} = \sum_{i=1}^{p} x_{ij} \widehat{\beta}_{i} = [\beta_{1}, ..., \beta_{P}] \begin{pmatrix} x_{i} \\ \vdots \\ x_{ip} \end{pmatrix} \quad , i = n+1, ..., n+m
$$
\n
$$
\frac{y_{i}}{1} = \sum_{i=1}^{p} x_{ij} \widehat{\beta}_{i} = [\beta_{1}, ..., \beta_{P}] \begin{pmatrix} x_{i} \\ \vdots \\ x_{ip} \end{pmatrix} \quad , i = m+1, ..., n+m
$$
\n
$$
\frac{y_{i}}{1} = \sum_{i=1}^{p} x_{ij} \widehat{\beta}_{i} = \frac{1}{2} \begin{pmatrix} \beta_{1}, ..., \beta_{P} \\ \vdots \\ \beta_{ip} \end{pmatrix} \begin{pmatrix} x_{i} \\ \vdots \\ x_{ip} \end{pmatrix}
$$
\n
$$
\frac{y_{i}}{1} = \sum_{i=1}^{p} x_{ij} \widehat{\beta}_{i} = \frac{1}{2} \begin{pmatrix} \beta_{1}, ..., \beta_{P} \\ \vdots \\ \beta_{ip} \end{pmatrix} \begin{pmatrix} x_{i} \\ \vdots \\ x_{ip} \end{pmatrix}
$$
\n
$$
\frac{y_{i}}{1} = \sum_{i=1}^{p} x_{ij} \widehat{\beta}_{i} = \sum_{i=1}^{p
$$

 $y^{(\prime)}$ 

 $y^{(2)}$ 

#### Fully-Connected Layer for 1D Signal



### Fully-Connected Layer for RGB Image

 $32x32x3$  image -> stretch to 3072 x 1



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#### **Convolutional Layer for ID Signal**







### Convolutional Layer for 2D Matrix/Image



## Convolutional Layer for RGB Image

## 32x32x3 image



### 5x5x3 filter



**Convolve the filter with the image** i.e. "slide over the image spatially, computing dot products"



A closer look at spatial dimensions:



For example, if we had six 5x5 filters, we'll get six separate *activation maps*:



We stack these up to get a "new image" of size 28x28x6!

## Building Block for Modern CNN



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CNN is composed of a sequence of convolutional layers, interspersed with activation functions (ReLU, in most cases).



(Fei-Fei Li et al., CS231n)



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## Residual Neural Network (ResNet) (Kaiming He et al., 2015)

- ◆ Skip connections or shortcuts are added.
- They can
	- **↑ avoid "vanishing gradients", and**
	- $\rightarrow$  make optimization landscape flatter.
- $\blacklozenge$  From Taylor expansion perspective, the neural network only learns the higher-order error terms beyond the linear term **x**.
- Has interpretations in PDE.
- Preferred modern NN structure.



$$
\mathbf{y} = \cdots \sigma \Big( \mathbf{W}_3 \left[ \mathbf{x} + \sigma \big( \mathbf{W}_2 \, \sigma (\mathbf{W}_1 \mathbf{x}) \big) \right] \Big) \cdots
$$

$$
g(\mathbf{x})
$$

Ex:

#### When Output is Categorical / Qualitative

- A softmax layer is needed:
- Softmax function:

$$
\sigma_i(\mathbf{z}) = \frac{e^{\beta z_i}}{\sum_{j=1}^{K} e^{\beta z_j}}
$$



conv/fully connected  $\leftarrow$   $\rightarrow$  softmax layer

Winner takes all!

### Other Essential Aspects of CNN

- ◆ Due to time constraints, this overview lecture covered only the structural elements of CNNs. Other essential aspects are:
	- Cost function/loss, e.g., MSE, cross entropy.
	- $\triangle$  How to train CNNs or estimate the weights (will only give practice code), i.e., backpropagation (will cover in the next two lectures).
	- $\rightarrow$  Practical training considerations including
		- How to determine number of hidden units/channels to be used,
		- How to tune learning rate and batch size, and
		- When to stop training (number of epochs).
- ◆ For a more complete treatment on CNN, refer to the dedicate courses such as [CS231n CNNs for Visual Recognition](https://www.youtube.com/playlist?list=PL3FW7Lu3i5JvHM8ljYj-zLfQRF3EO8sYv) or ECE 542/492.

# Machine Learning (ML) and Data Science (DS)

◆ Follow-up machine learning / data science courses:

ECE 542/492 Neural Networks (S'23)

- ECE 792-□ Advanced Topics in Machine Learning (S'23)
- ECE 592-61 Data Science (each fall)
- ECE 759 Pattern Recognition and Machine Learning (S'24)
- ECE 763 Computer Vision (S'24)
- Any courses/videos on YouTube, Coursera, etc.
- State-of-the-art theory & applications: ICML, NeurIPS, ICLR, AAAI
- ◆ Data science competitions: kaggle.com
- ◆ Programming languages for ML/DS: Python, R, Matlab

# Overview of Modern ML Applications: Recurrent Neural Network (RNN) and LSTM

 $\mathsf{V}$ 

**RNN** 

 $\mathsf{x}$ 

Acknowledgment: Some graphics and slides were adapted from Stanford's CS231n by Fei-Fei Li et al.: http://cs231n.stanford.edu/

## A Sequence of Identical Neural Network Modules

Force the neural nets (in green) to be the same to lower the complexity!



Image Captioning image -> seq of words

Emotion Classification seq of words -> emotion

Machine Translation seq of words -> seq of words

Video classification at frame level

# Recurrent Neural Network (RNN): Definition

We can process a sequence of vectors  $x$  by applying a recurrence formula at every time step:

$$
h_t=f_W(h_{t-1},x_t)\\
$$

 $h<sub>t</sub>$ : state,  $x<sub>t</sub>$ : input *f<sup>W</sup>* : neural network

$$
y_t = W_{hy} \mathcal{h}_t
$$



#### Recurrent Neural Network (RNN): Implementation

$$
h_t = f_W(h_{t-1},x_t)\\|\\h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)
$$

Diagram for *fW*. Can you label the details?



*f<sup>W</sup>* is implemented via

- linear transforms  $W_{hh}$  and  $W_{xh}$  and
- elementwise nonlinear function tanh(∙)

### Recurrent Neural Network (RNN): Unrolled



## Example: Character-Level Language Model



```
Vocabulary: 
[h, e, l, o]
```
At test time, sample characters one at a time, feed back to model



# Long Short-Term Memory (LSTM) Network

- ◆ RNN has the "vanishing gradient" problem!
- ◆ Resolved by long short-term memory (LSTM) units.



RNN  
\n
$$
h\left(W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}\right)
$$
\n
$$
h_{t} = \sigma\begin{pmatrix}i\\b\\c\\d\end{pmatrix} = \begin{pmatrix}\sigma\\c\\d\\tanh\end{pmatrix}W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}
$$
\n
$$
c_t = f \odot c_{t-1} + i \odot g
$$
\n
$$
h_t = o \odot \tanh(c_t)
$$

#### An LSTM Unit [Hochreiter et al., 1997]



# **Overview of Modern ML Applications:** Transformers and BERT



Acknowledgment: Some graphics and slides were adapted from https://peltarion.com/blog/data-science/self-attention-video

### How to make good sense of language?

- ◆ Reading comprehension: If you were Google, what result(s) should you return for "brazil traveler to usa need a visa"?
	- 1. A webpage on U.S. citizens traveling to Brazil
	- 2. A webpage of the U.S. embassy/consulate in Brazil
- ◆ Contextualization is the key!
	- $\rightarrow$  A nice walk by the river bank.
	- **← Walk to the bank and get cash.**

#### Word Embeddings in Natural Language Processing (NLP)

**Embedding vectors:** 

**WordPiece tokens:** 

Values are pretrained



Embedding examples: Bag of Words (BoW), Word2Vec, …

### Word Embeddings are Meaningful Under "+" and "−"



#### Contextualization by "Attention"





#### Similarity Measure via Inner Product



### Exponential Saturation & Normalization via Softmax



#### Contextualization via Linear Combination



# Key, Value, and Query

- ◆ "Key", "value", and "query" are three projections of an input embedding to three vector subspaces.
- ◆ Each subspace represents a unique semantic aspect.
- ◆ The projection operators / matrices provide trainable parameters for Transformer neural networks.



### Multi-Head Attention



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# Bidirectional Encoder Representations from Transformers (BERT)



# Neural Network Training: Backpropagation

Acknowledgment: Some graphics and slides were adapted from Profs. Jain (MSU), Min Wu (UMD), Fei-Fei Li (Stanford) Some figures are from Duda-Hart-Stork textbook, Fei-Fei Li's slides

### 3-Layer Neural Network Structure

- $\blacklozenge$  A single "bias unit" is connected to each unit in addition to the input units
- Net activation:

$$
net_{j} = \sum_{i=1}^{d} x_{i}w_{ji} + w_{j0} = \sum_{i=0}^{d} x_{i}w_{ji} \equiv w_{j}^{t}.x,
$$

where the subscript *i* indexes units in the input layer, *j* indexes units in the hidden layer;

*wji* denotes the input-to-hidden layer weights at hidden unit *j*.

#### $+$  In neurobiology, such weights or connections are called "synapses "

 $\triangleleft$  Each hidden unit emits an output that is a nonlinear function of its activation

$$
y_j = f(net_j)
$$



# Training Neural Networks / Estimating Weights

- Notations:  $t_k \sim$  the kth target (or desired) output,  $z_k \sim$  the kth estimated/computed output with  $k = 1, ..., c$ .  $w_{ij}$  ~ weight of the network
- Squared cost func:

$$
J(w) = \frac{1}{2} \sum_{k=1}^{c} (t_k - z_k)^2 = \frac{1}{2} ||t - z||^2
$$

*w*

- Learning based on gradient descent by iteratively updating the weights:  $w(m + 1) = w(m) + \Delta w(m)$ , *J*  $\Delta w = -\eta \frac{\partial}{\partial z}$ 
	- The weights are initialized with random values, and updated in a direction to reduce the error.
	- **Learning rate**, *n*, controls the step size of the update in weights.

*w*

∂

Walking man image is CC0 1.0 public domain<sup>1</sup> Figure source: Stanford CS231n by Fei-Fei Li



### Efficient Gradient Calculation: Backpropagation

- $\blacklozenge$  Computes  $\partial J / \partial w_{ii}$  for a single input-output pair.
- Exploit the chain rule for differentiation, e.g.,

$$
\frac{\partial J}{\partial w_{ji}} = \frac{\partial J}{\partial y_j} \cdot \frac{\partial y_j}{\partial net_j} \cdot \frac{\partial net_j}{\partial w_{ji}}
$$

- ◆ Computed by forward and backward sweeps over the network, keeping track only of quantities local to each unit.
- $\blacklozenge$  Iterate backward one unit at a time from last layer. Backpropagation avoids redundant calculations.

#### Backpropagation (BP): An Example



# Network Learning by BP (cont'd)

 $\triangle$  Error on hidden-to-output weight:



 $\blacklozenge$ *b*<sub>*k*</sub>, the sensitivity of unit *k* :

describes how the overall error changes with the activation of the unit's net activation





$$
\delta_k = -\frac{\partial J}{\partial net_k} = -\frac{\partial J}{\partial z_k} \cdot \frac{\partial z_k}{\partial net_k} = (t_k - z_k) f'(net_k)
$$
  
\n
$$
\star \text{ Since } net_k = w_k^{\text{t}} y \text{, we have } \frac{\partial net_k}{\partial w_{kj}} = y_j
$$

**★ Summary I:** weight update (or learning rule) for the hidden-to-output weight is:

$$
\Delta w_{kj} = \eta (t_k - z_k) f'(net_k) y_j = \eta \delta_k y_j
$$

# Network Learning by BP (cont'd)

∂

 $k=1$  *CHEL*<sub>k</sub> *Cy*<sub>j</sub>  $k=1$ 

*k*

Error on input-to-hidden weight:

• chain rule: 
$$
\frac{\partial J}{\partial w_{ji}} = \frac{\partial J}{\partial y_j} \cdot \frac{\partial y_j}{\partial net_j} \cdot \frac{\partial net_j}{\partial w_{ji}}
$$

$$
\frac{\partial J}{\partial y_j} = \frac{\partial}{\partial y_j} \left[ \frac{1}{2} \sum_{k=1}^{c} (t_k - z_k)^2 \right] = - \sum_{k=1}^{c} (t_k - z_k) \frac{\partial z_k}{\partial y_j}
$$
  
= 
$$
- \sum_{k=1}^{c} (t_k - z_k) \frac{\partial z_k}{\partial net_k} \cdot \frac{\partial net_k}{\partial y_j} = - \sum_{k=1}^{c} (t_k - z_k) f'(net_k) w
$$

*j*



 Sensitivity of a hidden unit: (Similarly defined as earlier)

$$
\delta_j \equiv \frac{\partial J}{\partial net_j} = f'(net_j) \sum_{k=1}^c w_{kj} \delta_k
$$

 $k \sim k$  *J*  $j \sim k$   $\frac{1}{k}$   $\frac{1}{k}$ 

 Summary 2: Learning rule for the input-to-hidden weight is:  $\Delta w_{ji} = \eta \left[ f'(net_j) \Sigma w_{kj} \delta_k \right]$  $\mathfrak{o}_j$  $x_i = \eta \delta_j x$ 

#### Sensitivity at Hidden Node



Figure 6.5: The sensitivity at a hidden unit is proportional to the weighted sum of the sensitivities at the output units:  $\delta_j = f'(net_j) \sum_{k=1}^{\infty} w_{kj} \delta_k$ . The output unit sensitivities are thus propagated "back" to the hidden units.

# BP Algorithm: Training Protocols

- ◆ Training protocols:
	- **← Batch:** Present all patterns before updating weights
	- **→ Stochastic: patterns/input are chosen randomly from training set; network weights** are updated for each pattern
	- ◆ Online: present each pattern once & only once (no memory for storing patterns)

◆ Stochastic backpropagation algorithm:

Begin initialize  $n_H$ ; w, criterion thres,  $\eta$ ,  $m \leftarrow \emptyset$ do  $m \leftarrow m + 1$  $x^m$   $\leftarrow$  randomly chosen pattern  $w_{ji} \leftarrow w_{ji} + \eta \delta_j x_i$ ;  $w_{kj} \leftarrow w_{kj} + \eta \delta_k y_j$ until ||∇J(w)|| < thres return w End

# BP Algorithm: Stopping Criterion

- Algorithm terminates when the change in criterion function *J*(*w*) is smaller than some preset thres
	- Also exist other stopping criteria with better performance
- A weight update may reduce the error on the single pattern being presented, but can increase the error on the full training set
	- ◆ In stochastic backpropagation and batch propagation, we should make several passes (epoches) through the training data

# Learning Curves

- $\rightarrow$  Before training starts, the error on the training set is high; as the learning proceeds, error becomes smaller
- $\div$  Error per pattern depends on the amount of training data and expressive power (e.g. # of weights) in the network
- **← Average error on an independent test** set is always higher than on the training set, and it can decrease or increase





- $\rightarrow$  A validation set is used in order to decide when to stop training:
	- Avoid overfitting the network and decrease the power of the classifier's generalization

#### "Stop training when the error on the validation set is minimum"

## Practical Considerations: Learning Rate

- ◆ Learning Rate
	- $\triangle$  Small learning rate: slow convergence
	- Large learning rate: high oscillation and slow convergence



Figure 6.18: Gradient descent in a one-dimensional quadratic criterion with different learning rates. If  $\eta < \eta_{\text{opt}}$ , convergence is assured, but training can be needlessly slow. If  $\eta = \eta_{\text{opt}}$ , a single learning step suffices to find the error minimum. If  $\eta_{opt} < \eta < 2\eta_{opt}$ , the system will oscillate but nevertheless converge, but training is needlessly slow. If  $\eta > 2\eta_{opt}$ , the system diverges.